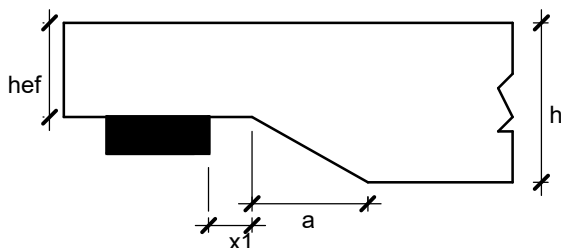
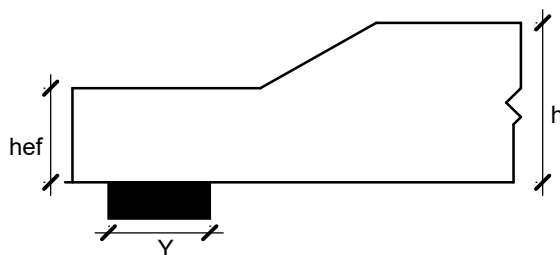


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Joist section design



End notch type (a)



End notch type (b)

Calculations for timber joists are in accordance with BS EN 1995-1-1:2004+A1:2008

Timber size	- 63 mm wide x 200 mm deep
Span of joist	SPAN = 2.4 m
Number of pieces	np = 1
End bearing	- left hand end
	- Right hand end
Strength class from Table 1	- C16
Service class	- 2 (Covered and heated or unheated)
Variable load duration	- Medium term
Load sharing	- No

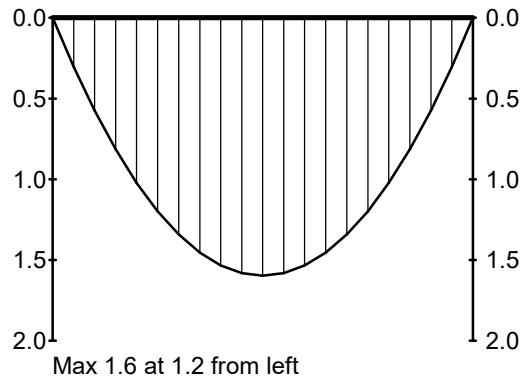
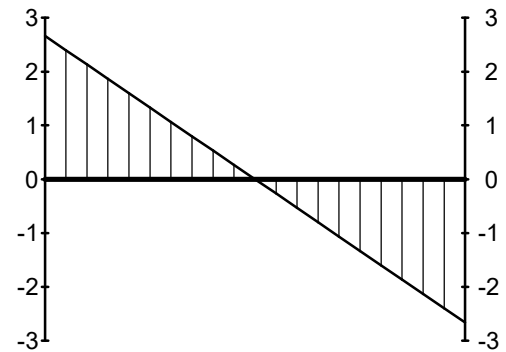
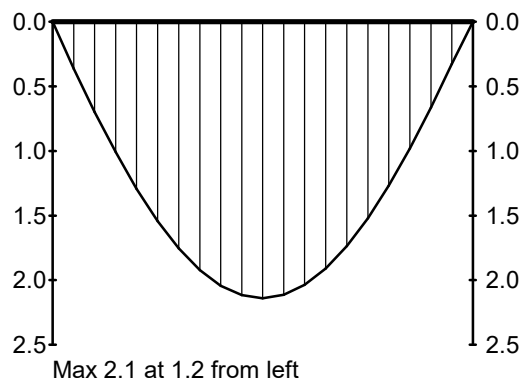
Notches details

End notches	- left hand end	- none specified
	- right hand end	- none specified

Design effects

Moment due to permanent load	MEdGd	= 0.301 kNm
Moment due to variable load	MEdQd	= 1.296 kNm
Shear due to permanent load at left support	VEdGd,L	= 0.502 kN
Shear due to variable load load at left support	VEdQd,L	= 2.16 kN
Shear due to permanent load at right support	VEdGd,R	= 0.502 kN
Shear due to variable load load at right support	VEdQd,R	= 2.16 kN
Deflection due to permanent load	U,Gk	= 0.439 mm
Deflection due to variable load	U,Qk	= 1.7 mm

Load Description	Type	A	B	C	Gk	Qk
Beam Loading	UDL	0	2.4		0.31	1.2

Moment (1.35Gk+1.5Qk) kNm**Shear (1.35Gk+1.5Qk) kN** (2.66) (-2.66)**Deflection (1.0Gk+1.0Qk) mm****Section properties**

Area

A = 12600 mm²

Section modulus

W_y = 420000 mm³

Second moment of area

I_y = 42000000 mm⁴**Grade stresses - from Table 1 of EN 338:2009**

Bending stress

f_{m,k} = 16 N/mm²

Tension stress parallel to grain

f_{t,0,k} = 10 N/mm²

Tension stress perpendicular to grain

f_{t,90,k} = 0.4 N/mm²

Compression stress parallel to grain

f_{c,0,k} = 17 N/mm²

Compression stress perpendicular to grain

f_{c,90,k} = 2.2 N/mm²

Shear stress

f_{v,k} = 3.2 N/mm²

Mean modulus of elasticity parallel

E_{mean} = 8 kN/mm²

5% modulus of elasticity parallel

E_{0.05} = 5.4 kN/mm²

Mean shear modulus

G_{mean} = 0.5 kN/mm²

Density

ρ_k = 310 kg/m³**Modification factors**

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Depth factor	kh	= 1
Load duration factor (Table 3.1)	kmod	= 0.8
Permanent load duration factor (Table 3.1)	kmodp	= 0.6
System length factor (cl 6.6 of EN 1995)	ksys	= 1
Reduced bending stress factor (cl 6.3.3)	kcrit	= 1
Load configuration factor (cl 6.1.5)	kc,90	= 1.5
Shear crack factor (cl 6.1.7)	kcr	= 0.67
Deformation factor (Table 3.2)	kdef	= 0.8

Partial safety factors

Material safety factor	γ_M	= 1.3
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Bending check

Bending Stresses

Bending stress due to permanent load

$$\sigma_{mydGd} = MEdGd \cdot 10^6 / W_y$$

$$= 0.717 \text{ N/mm}^2$$

Bending stress due to variable load

$$\sigma_{mydQd} = MEdQd \cdot 10^6 / W_y$$

$$= 3.086 \text{ N/mm}^2$$

Total bending stress

$$\sigma_{myd} = \sigma_{mydGd} + \sigma_{mydQd}$$

$$= 3.803 \text{ N/mm}^2$$

Design bending strength

$$f_{md} = f_{mk} \cdot k_h \cdot k_{mod} \cdot k_{sys} \cdot k_{crit} / \gamma_M$$

$$= 9.846 \text{ N/mm}^2$$

Bending stress utilisation

$$U_{bm} = \sigma_{myd} / f_{md}$$

$$= 0.386$$

Bending status - **PASS.**

Shear check

Left support

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Shear stress due to total permanent load

$$\begin{aligned}\tau_{dGdl} &= 1.5 \cdot (V_{EdGd,L} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef,L} \cdot n_p) \\ &= 0.0892 \text{ N/mm}^2\end{aligned}$$

Shear stress due to total variable load

$$\begin{aligned}\tau_{dQdl} &= 1.5 \cdot (V_{EdQd,L} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef,L} \cdot n_p) \\ &= 0.384 \text{ N/mm}^2\end{aligned}$$

Total shear stress

$$\begin{aligned}\tau_{dl} &= \tau_{dGdl} + \tau_{dQdl} \\ &= 0.473 \text{ N/mm}^2\end{aligned}$$

Design shear strength

$$\begin{aligned}f_{vdl} &= f_{vk} \cdot k_{mod} \cdot k_{sys} \cdot K_{vL} / \gamma_M \\ &= 1.969 \text{ N/mm}^2\end{aligned}$$

Shear utilisation

$$\begin{aligned}U_{shl} &= \tau_{dl} / f_{vdl} \\ &= 0.24\end{aligned}$$

Shear status at left support - **PASS.**

Right support

Shear stress due to total permanent load

$$\begin{aligned}\tau_{dGdr} &= 1.5 \cdot (V_{EdGd,R} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef,R} \cdot n_p) \\ &= 0.0892 \text{ N/mm}^2\end{aligned}$$

Shear stress due to total variable load

$$\begin{aligned}\tau_{dQdr} &= 1.5 \cdot (V_{EdQd,R} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef,R} \cdot n_p) \\ &= 0.384 \text{ N/mm}^2\end{aligned}$$

Total shear stress

$$\begin{aligned}\tau_{dr} &= \tau_{dGdr} + \tau_{dQdr} \\ &= 0.473 \text{ N/mm}^2\end{aligned}$$

Design shear strength

$$\begin{aligned}f_{vdr} &= f_{vk} \cdot k_{mod} \cdot k_{sys} \cdot K_{vR} / \gamma_M \\ &= 1.969 \text{ N/mm}^2\end{aligned}$$

Shear utilisation

$$\begin{aligned}U_{shr} &= \tau_{dr} / f_{vdr} \\ &= 0.24\end{aligned}$$

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Shear status at right support - **PASS.**

Bearing check

Left support bearing check

Bearing contact length

$$c_l = Y_l + \min_{\text{bear}} = 80 \text{ mm}$$

Bearing stress due to permanent load

$$\sigma_{c90dGdI} = V_{EdGd,L} \cdot 10^3 / (b \cdot c_l \cdot n_p) = 0.0996 \text{ N/mm}^2$$

Bearing stress due to variable load

$$\sigma_{c90dQdI} = V_{EdQd,L} \cdot 10^3 / (b \cdot c_l \cdot n_p) = 0.429 \text{ N/mm}^2$$

Total bearing stress

$$\sigma_{c90dI} = \sigma_{c90dGdI} + \sigma_{c90dQdI} = 0.528 \text{ N/mm}^2$$

Design bearing strength

$$f_{c90dI} = f_{c90k} \cdot k_{\text{mod}} \cdot k_{\text{sys}} \cdot k_{c,90} / \gamma_M = 2.031 \text{ N/mm}^2$$

Bearing stress utilisation

$$U_{bI} = \sigma_{c90dI} / f_{c90dI} = 0.26$$

Bearing status at left support - **PASS.**

Right support bearing check

Bearing contact length

$$c_l = Y_r + \min_{\text{bear}} = 80 \text{ mm}$$

Bearing stress due to permanent load

$$\sigma_{c90dGdr} = V_{EdGd,R} \cdot 10^3 / (b \cdot c_l \cdot n_p) = 0.0996 \text{ N/mm}^2$$

Bearing stress due to variable load

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	$\sigma_{c90dQdr}$	$= VEdQd,R*10^3/(b*cl*np)$ $= 0.429 \text{ N/mm}^2$
Total bearing stress	σ_{c90dr}	$= \sigma_{c90dGdr} + \sigma_{c90dQdr}$ $= 0.528 \text{ N/mm}^2$
Design bearing strength	fc_{90dr}	$= fc_{90k}*k_{mod}*k_{sys}*k_{c,90}/\gamma_M$ $= 2.031 \text{ N/mm}^2$
Bearing stress utilisation	U_{br}	$= \sigma_{c90dr}/fc_{90dr}$ $= 0.26$
Bearing status at right support - PASS .		
Deflection check		
Section properties used to calculate bending and shear deflection		
Second moment of area	I	$= 4200 \text{ mm}^4$
Modulus of elasticity	E_{mean}	$= 8000 \text{ N/mm}^2$
Area	A	$= 126 \text{ mm}^2$
Shear modulus	G_{mean}	$= 500 \text{ N/mm}^2$
Section factor	F	$= 1.2 \text{ (For rectangular section)}$
Final deflection due to permanent load,	U_{fnG}	$= U_{Gk}*(1+k_{def})$ $= 0.791 \text{ mm}$
Final deflection due to variable load,	U_{fnQ}	$= U_{Qk}*(1+(k_{def}*\psi_{21}))$ $= 2.109 \text{ mm}$
Total deflection,		

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U_{fin} = $U_{fnG} + U_{fnQ}$
= 2.899 mm

Allowable deflection,
 U_{allow} = $SPAN * 1000 / 250$
= 9.6 mm

Deflection utilisation,
 U_{def} = U_{fin} / U_{allow}
= 0.302

Deflection status - **PASS.**

Vibration check

[Expression 7.5 of BS EN 1995-1-1:2004+A1:2008]

Fundamental frequency
 f_1 = $18 / \sqrt{U_{fnG}}$
= 20.243 Hertz

Since $f_1 > 8$, Vibration status - **PASS.**

The section 63 x 200 mm PASSES all checks