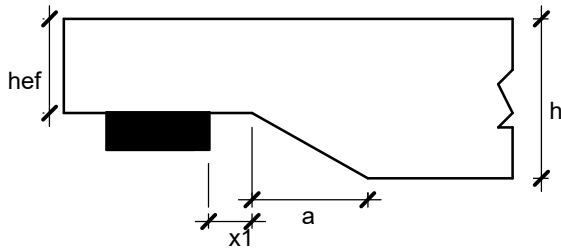
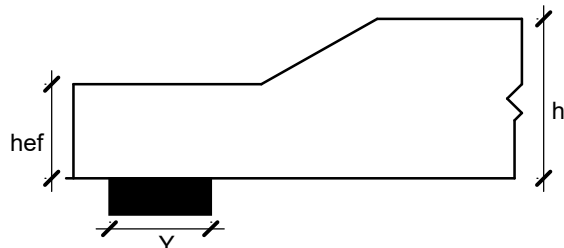


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Joist section design



End notch type (a)



End notch type (b)

Calculations for timber joists are in accordance with BS EN 1995-1-1:2004+A1:2008

Timber size	- 47 mm wide x 150 mm deep
Span of joist	SPAN = 0.6 m
Number of pieces	np = 1
End bearing	- left hand end - Right hand end
Strength class from Table 1	- C16
Service class	- 2 (Covered and heated or unheated)
Variable load duration	- Short term
Load sharing	- No

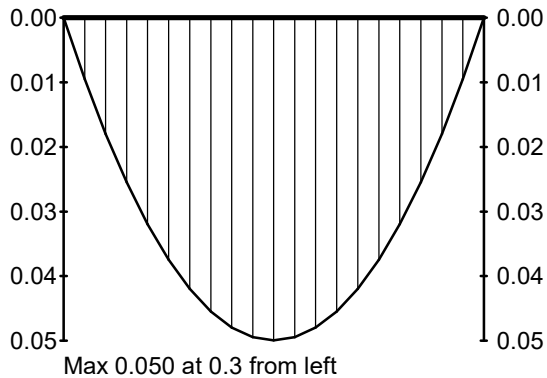
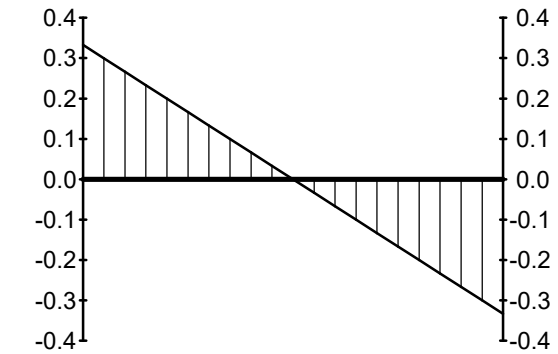
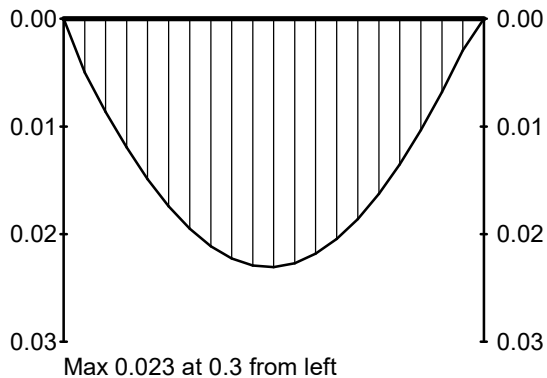
Notches details

End notches	- left hand end	- none specified
	- right hand end	- none specified

Design effects

Moment due to permanent load	MEdGd	= 0 kNm
Moment due to variable load	MEdQd	= 0.05 kNm
Shear due to permanent load at left support	VEdGd,L	= 0 kN
Shear due to variable load load at left support	VEdQd,L	= 0.333 kN
Shear due to permanent load at right support	VEdGd,R	= 0 kN
Shear due to variable load load at right support	VEdQd,R	= 0.333 kN
Deflection due to permanent load	U,Gk	= 0 mm
Deflection due to variable load	U,Qk	= 0.0231 mm

Load Description	Type	A	B	C	Gk	Qk
Horizontal load	UDL	0	0.6		0.0	0.74

Moment (1.35Gk+1.5Qk) kNm**Shear (1.35Gk+1.5Qk) kN****Deflection (1.0Gk+1.0Qk) mm****Section properties**

Area

A = 7050 mm²

Section modulus

W_y = 176250 mm³

Second moment of area

I_y = 13218750 mm⁴**Grade stresses - from Table 1 of EN 338:2009**

Bending stress

f_{m,k} = 16 N/mm²

Tension stress parallel to grain

f_{t,0,k} = 10 N/mm²

Tension stress perpendicular to grain

f_{t,90,k} = 0.4 N/mm²

Compression stress parallel to grain

f_{c,0,k} = 17 N/mm²

Compression stress perpendicular to grain

f_{c,90,k} = 2.2 N/mm²

Shear stress

f_{v,k} = 3.2 N/mm²

Mean modulus of elasticity parallel

E_{mean} = 8 kN/mm²

5% modulus of elasticity parallel

E_{0.05} = 5.4 kN/mm²

Mean shear modulus

G_{mean} = 0.5 kN/mm²

Density

ρ_k = 310 kg/m³**Modification factors**

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Depth factor	kh	= 1
Load duration factor (Table 3.1)	kmod	= 0.9
Permanent load duration factor (Table 3.1)	kmodp	= 0.6
System length factor (cl 6.6 of EN 1995)	ksys	= 1
Reduced bending stress factor (cl 6.3.3)	kcrit	= 1
Load configuration factor (cl 6.1.5)	kc,90	= 1.5
Shear crack factor (cl 6.1.7)	kcr	= 0.67
Deformation factor (Table 3.2)	kdef	= 0.8

Partial safety factors

Material safety factor	γ_M	= 1.3
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Bending check

Bending Stresses

Bending stress due to permanent load

$$\sigma_{mydGd} = MEdGd \cdot 10^6 / Wy$$

$$= 0 \text{ N/mm}^2$$

Bending stress due to variable load

$$\sigma_{mydQd} = MEdQd \cdot 10^6 / Wy$$

$$= 0.283 \text{ N/mm}^2$$

Total bending stress

$$\sigma_{myd} = \sigma_{mydGd} + \sigma_{mydQd}$$

$$= 0.283 \text{ N/mm}^2$$

Design bending strength

$$fmd = fmk \cdot kh \cdot kmod \cdot ksys \cdot kcrit / \gamma_M$$

$$= 11.077 \text{ N/mm}^2$$

Bending stress utilisation

$$U_{bm} = \sigma_{myd} / fmd$$

$$= 0.0256$$

Bending status - **PASS.**

Shear check

Left support

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Shear stress due to total permanent load

$$\tau_{dGdl} = 1.5 \cdot (V_{EdGd,L} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef_L} \cdot n_p)$$

$$= 0 \text{ N/mm}^2$$

Shear stress due to total variable load

$$\tau_{dQdl} = 1.5 \cdot (V_{EdQd,L} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef_L} \cdot n_p)$$

$$= 0.106 \text{ N/mm}^2$$

Total shear stress

$$\tau_{dl} = \tau_{dGdl} + \tau_{dQdl}$$

$$= 0.106 \text{ N/mm}^2$$

Design shear strength

$$f_{vdl} = f_{vk} \cdot k_{mod} \cdot k_{sys} \cdot K_{vL} / \gamma_M$$

$$= 2.215 \text{ N/mm}^2$$

Shear utilisation

$$U_{shl} = \tau_{dl} / f_{vdl}$$

$$= 0.0477$$

Shear status at left support - **PASS.**

Right support

Shear stress due to total permanent load

$$\tau_{dGdr} = 1.5 \cdot (V_{EdGd,R} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef_R} \cdot n_p)$$

$$= 0 \text{ N/mm}^2$$

Shear stress due to total variable load

$$\tau_{dQdr} = 1.5 \cdot (V_{EdQd,R} \cdot 10^3) / (k_{cr} \cdot b \cdot h_{ef_R} \cdot n_p)$$

$$= 0.106 \text{ N/mm}^2$$

Total shear stress

$$\tau_{dr} = \tau_{dGdr} + \tau_{dQdr}$$

$$= 0.106 \text{ N/mm}^2$$

Design shear strength

$$f_{vdr} = f_{vk} \cdot k_{mod} \cdot k_{sys} \cdot K_{vR} / \gamma_M$$

$$= 2.215 \text{ N/mm}^2$$

Shear utilisation

$$U_{shr} = \tau_{dr} / f_{vdr}$$

$$= 0.0477$$

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Shear status at right support - **PASS.**

Bearing check

Left support bearing check

Bearing contact length

$$cl = Y_l + \text{minbear}$$

$$= 80 \text{ mm}$$

Bearing stress due to permanent load

$$\sigma_{c90dGdl} = VEd_{Gd,L} \cdot 10^3 / (b \cdot cl \cdot n_p)$$

$$= 0 \text{ N/mm}^2$$

Bearing stress due to variable load

$$\sigma_{c90dQdl} = VEd_{Qd,L} \cdot 10^3 / (b \cdot cl \cdot n_p)$$

$$= 0.0886 \text{ N/mm}^2$$

Total bearing stress

$$\sigma_{c90dl} = \sigma_{c90dGdl} + \sigma_{c90dQdl}$$

$$= 0.0886 \text{ N/mm}^2$$

Design bearing strength

$$fc_{90dl} = f_{c90k} \cdot k_{mod} \cdot k_{sys} \cdot k_{c,90} / \gamma_M$$

$$= 2.285 \text{ N/mm}^2$$

Bearing stress utilisation

$$U_{bl} = \sigma_{c90dl} / fc_{90dl}$$

$$= 0.0388$$

Bearing status at left support - **PASS.**

Right support bearing check

Bearing contact length

$$cl = Y_r + \text{minbear}$$

$$= 80 \text{ mm}$$

Bearing stress due to permanent load

$$\sigma_{c90dGdr} = VEd_{Gd,R} \cdot 10^3 / (b \cdot cl \cdot n_p)$$

$$= 0 \text{ N/mm}^2$$

Bearing stress due to variable load

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	$\sigma_{c90dQdr}$	= $VEdQd,R \cdot 10^3 / (b \cdot cl \cdot np)$ = 0.0886 N/mm ²
Total bearing stress	σ_{c90dr}	= $\sigma_{c90dGdr} + \sigma_{c90dQdr}$ = 0.0886 N/mm ²
Design bearing strength	fc_{90dr}	= $fc_{90k} \cdot k_{mod} \cdot k_{sys} \cdot k_{c,90} / \gamma_M$ = 2.285 N/mm ²
Bearing stress utilisation	U_{br}	= $\sigma_{c90dr} / fc_{90dr}$ = 0.0388
Bearing status at right support - PASS .		
Deflection check		
Section properties used to calculate bending and shear deflection		
Second moment of area	I	= 1320 mm ⁴
Modulus of elasticity	E_{mean}	= 8000 N/mm ²
Area	A	= 70.5 mm ²
Shear modulus	G_{mean}	= 500 N/mm ²
Section factor	F	= 1.2 (For rectangular section)
Final deflection due to permanent load,	U_{fnG}	= $U_{Gk} \cdot (1 + k_{def})$ = 0 mm
Final deflection due to variable load,	U_{fnQ}	= $U_{Qk} \cdot (1 + (k_{def} \cdot \psi_{21}))$ = 0.0286 mm
Total deflection,		

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	U_{fin}	$= U_{fnG} + U_{fnQ}$ $= 0.0286 \text{ mm}$
Allowable deflection,	U_{allow}	$= \text{SPAN} * 1000 / 250$ $= 2.4 \text{ mm}$
Deflection utilisation,	U_{def}	$= U_{fin} / U_{allow}$ $= 0.0119$

Deflection status - **PASS.**

The section 47 x 150 mm **PASSES** all checks